

Robust measurements of galaxy morphology with LSST

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How do galaxies evolve?

star-forming



disk-dominated

star formation

quenching mechanism = ????

morphology

quiescent



bulge-dominated

How do galaxies evolve?

star-forming



disk-dominated

gas: hydrodynamics
star formation

quenching mechanism = ????

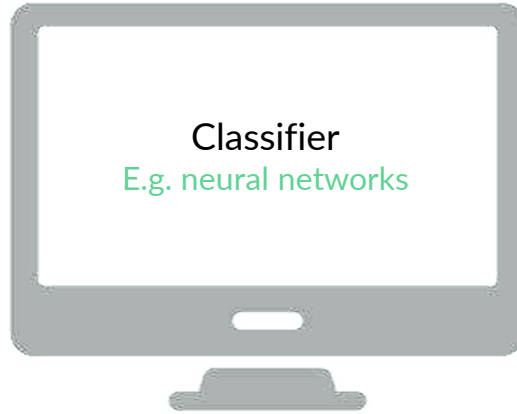
morphology
stars: gravity

quiescent



bulge-dominated

Why quantitative morphology?



Merger / non-
merger

Why quantitative morphology?



Disk / bulge
strength
C, Sersic n, B/T

Tidal features
A_s, outer A

Internal
disturbances
(e.g. dust lanes)
A + A_s in different bands

Different merger
stages
A, A_s, G/M20

Why quantitative morphology?



Disk / bulge
strength
C, Sersic n, B/T

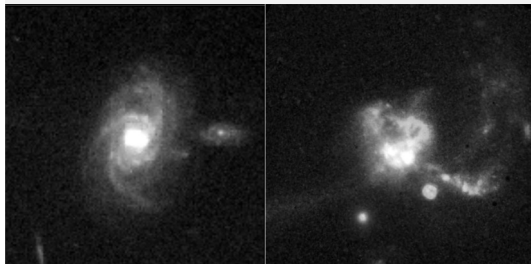
Tidal features
As, outer A

Internal
disturbances
(e.g. dust lanes)
A + As in different bands

Different merger
stages
A, As, G/M20

- + *Continuous* distributions let us study galaxy structure as a *function* of their environment/physical properties/etc

Disturbance



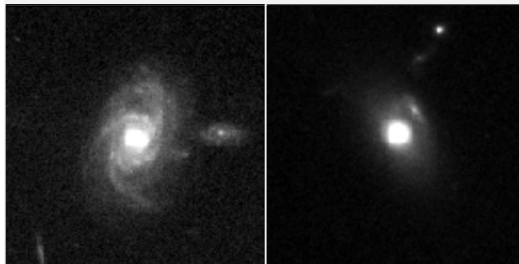
Non
parametric

Asymmetry
Shape asymmetry
G/M₂₀ disturbance
Shape asymmetry

Model
dependent

Residual Flux Fraction [RFF]

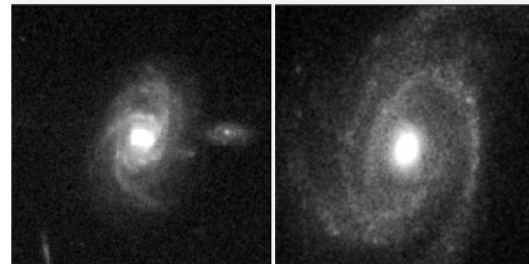
Bulge strength



Concentration
G/M₂₀ bulge strength

Sérsic index
Bulge-to-disk ratio [B/T]

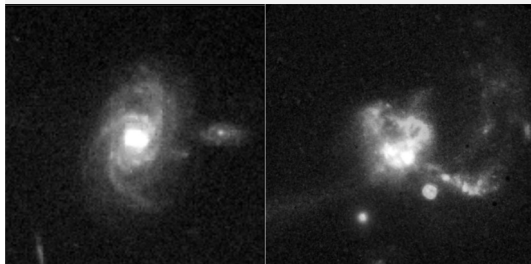
Size



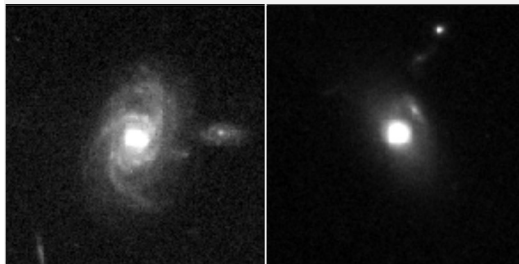
Petrosian radius
Compactness

Sérsic radius

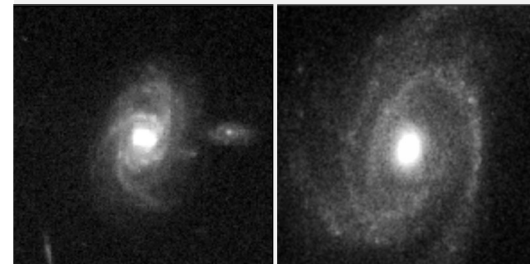
Disturbance



Bulge strength



Size



Non
parametric

Asymmetry

Shape

G/M₂₀

Shape asymmetry

A million definitions + implementations
Inconsistent measurements across different studies!

Model
dependent

Residual Flux Fraction [RFF]

Sérsic index

Bulge-to-disk ratio [B/T]

Sérsic radius

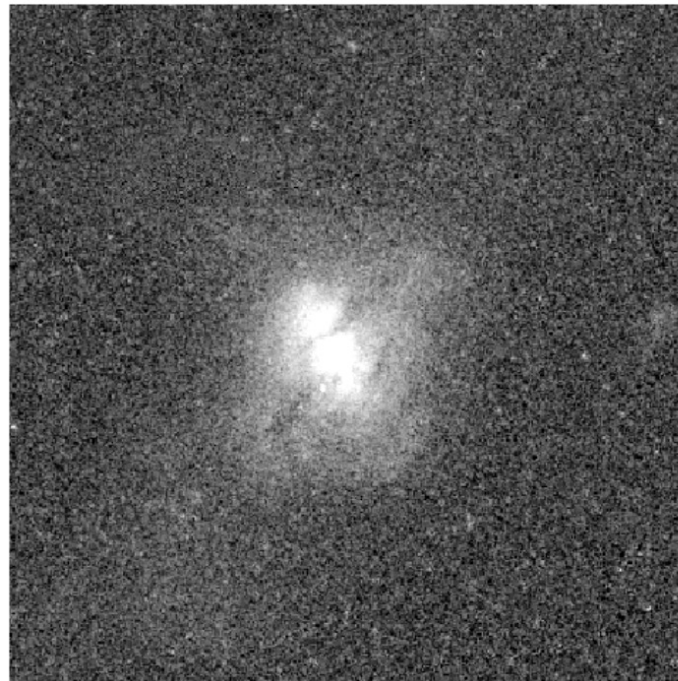
Case study: asymmetry

Conselice et al. (2003)

$$A = \frac{\sum |f - f^{180}| - N \langle A_{bg} \rangle}{\sum |f|}$$

image rotated image
background
asymmetry

Important in detecting mergers,
dust lanes, etc...

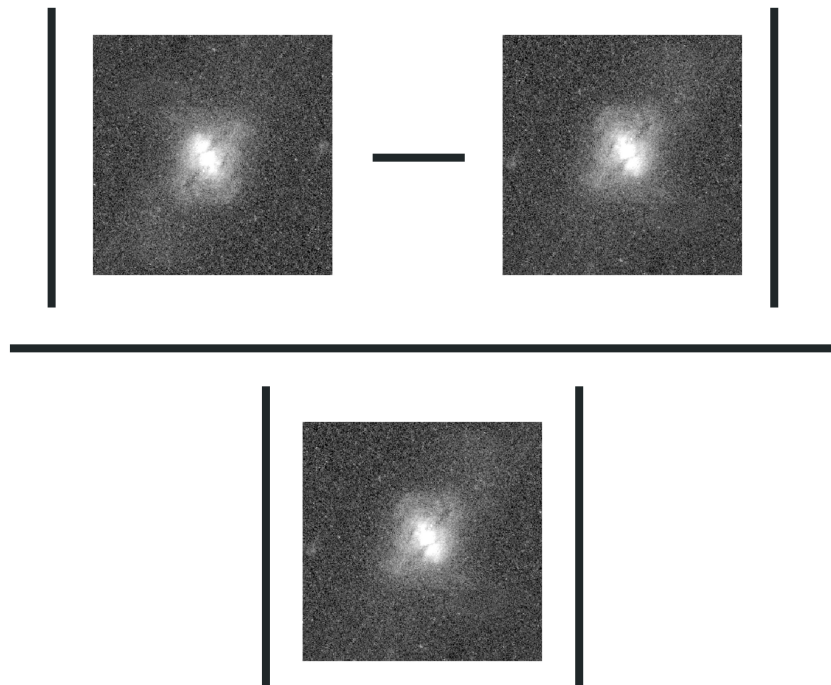


What's up with asymmetry?

Conselice et al. (2003)

$$A = \frac{\sum |f - f^{180}| - N \langle A_{bg} \rangle}{\sum |f|}$$

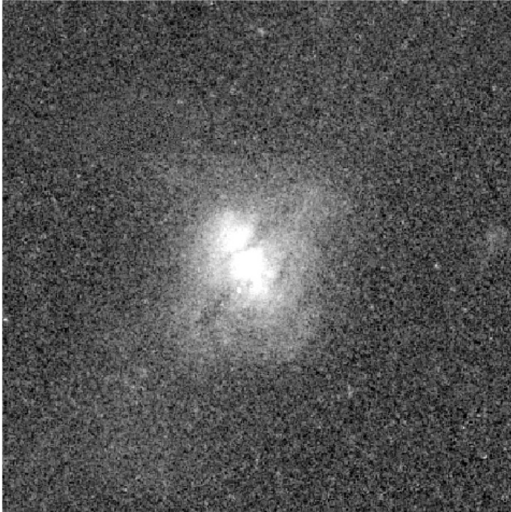
image rotated image
background
asymmetry



What's up with asymmetry?

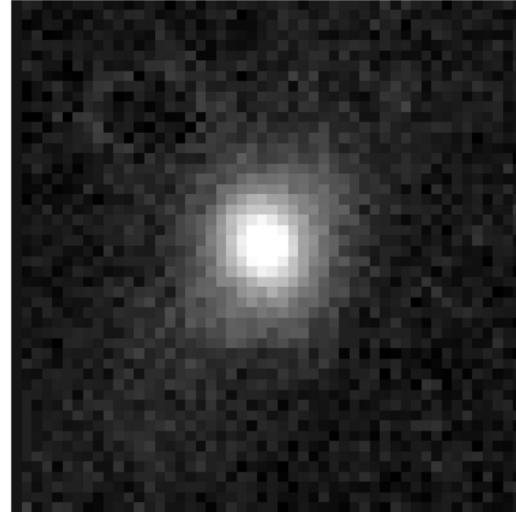
Conselice et al. (2003)

HST *R*-band



$A = 0.35$

SDSS *r*-band

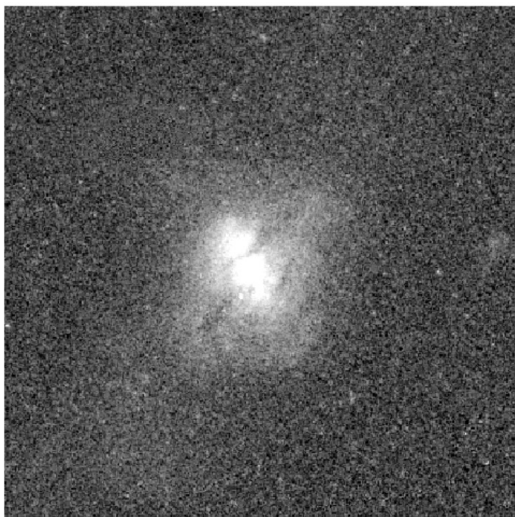


$A = 0.11$

What's up with asymmetry?

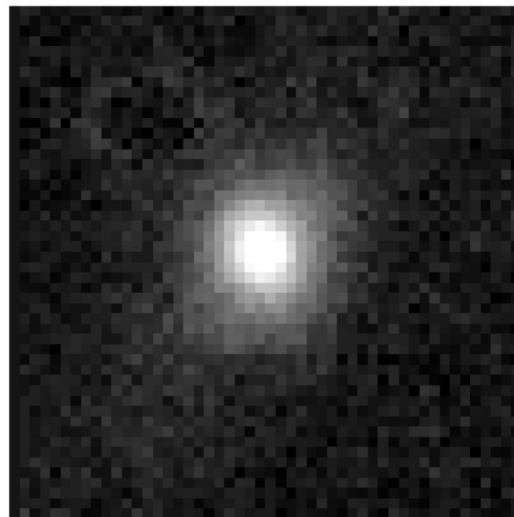
Conselice et al. (2003)

HST *R*-band



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SDSS *r*-band



$A = 0.11$

LSST imaging will still have high seeing (~ 0.5 of SDSS) and a *variable* image depth across the survey lifetime!

What's up with asymmetry?

Conselice et al. (2003)

$$A = \frac{\sum |f - f^{180}| - N \langle A_{bg} \rangle}{\sum |f|}$$

image rotated image
background asymmetry

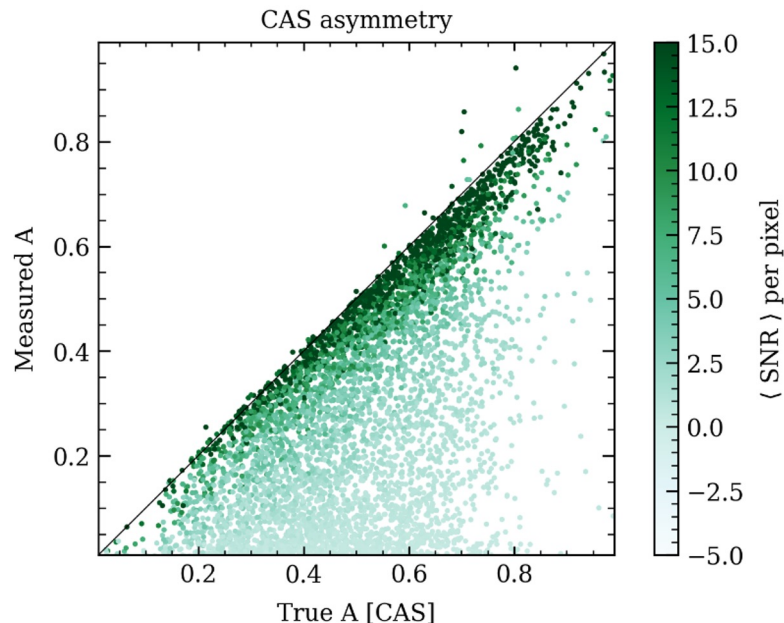
Only tested statistically in a few studies

Lotz et al. 2004, Thorp et al. 2021

Depends strongly on noise & resolution

But how much? And why?

**We need to understand these measurements better
before we commit to measuring them for 10^6 galaxies**



Asymmetry squared

$$A = \frac{\sum |f - f^{180}| - N\langle A_{bg} \rangle}{\sum |f|}$$

image rotated image
background asymmetry



$$A = \frac{\sum (f - f^{180})^2 - N\langle A_{bg}^2 \rangle}{\sum f^2 - N\langle f_{bg}^2 \rangle}$$

background flux correction

Better normalization

Normalization used to include a non-zero noise contribution, making asymmetry aperture size-dependent

Better behaviour with noisy images

Gaussian noise completely decoupled from the source asymmetry

Asymmetry squared: why?

$$\begin{array}{c} \text{image} \\ f \end{array} = \begin{array}{c} \text{source} \\ \lambda \end{array} * \begin{array}{c} f_s \\ \text{PSF} \end{array} + \begin{array}{c} \sigma \\ \text{noise} \end{array}$$

Source image

An observation is made from a source image by convolving it with a PSF and adding noise.

Asymmetry squared: why?

$$f = \underset{\text{PSF}}{\lambda} * \overset{\text{source}}{f_s} + \underset{\text{noise}}{\sigma}$$

CAS asymmetry:

$$|f - f^{180}| = |\lambda * (f_s - f_s^{180}) + (\sigma - \sigma^{180})|$$

$$\neq |\lambda * (f_s - f_s^{180})| + |\sigma - \sigma^{180}|$$

Background contribution is **not** separable

Source image

An observation is made from a **source image** by convolving it with a **PSF** and adding **noise**.

CAS asymmetry

Absolute value calculation does not allow you to separate the noise term and recover the real asymmetry

Asymmetry squared: why?

$$f = \lambda * f_s + \sigma$$

source
PSF noise

CAS asymmetry:

$$A = \frac{\sum |f - f^{180}| - N \langle A_{bg} \rangle}{\sum |f|}$$

image rotated image
background asymmetry

this term
doesn't do
much good...

Source image

An observation is made from a source image by convolving it with a PSF and adding noise.

CAS asymmetry

Absolute value calculation does not allow you to separate the noise term and recover the real asymmetry

Asymmetry squared: why?

$$f = \underset{\text{PSF}}{\lambda} * \overset{\text{source}}{f_s} + \underset{\text{noise}}{\sigma}$$

Squared asymmetry:

$$(f - f^{180})^2 = \lambda^2 * (f_s - f_s^{180})^2 + (\sigma - \sigma^{180})^2 + 2(\sigma - \sigma^{180}) \times \lambda * (f_s - f_s^{180})$$

This term is 0 when the image is background-subtracted!

The background term is **separable**

Source image

An observation is made from a **source image** by convolving it with a **PSF** and adding **noise**.

Better behaviour with noisy images

Gaussian noise completely decoupled from the source asymmetry


Asymmetry squared: why?

$$f = \underbrace{\lambda}_{\text{PSF}} * \underbrace{f_s}_{\text{source}} + \underbrace{\sigma}_{\text{noise}}$$

Squared asymmetry:

$$A = \frac{\sum (f - f^{180})^2 - N \langle A_{bg}^2 \rangle}{\sum f^2 - N \langle f_{bg}^2 \rangle}$$

This term
recovers
source
asymmetry!



Source image

An observation is made from a **source image** by convolving it with a **PSF** and adding **noise**.

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Asymmetry squared

$$A = \frac{\sum |f - f^{180}| - N\langle A_{bg} \rangle}{\sum |f|}$$

image rotated image background asymmetry



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background flux correction

Better normalization

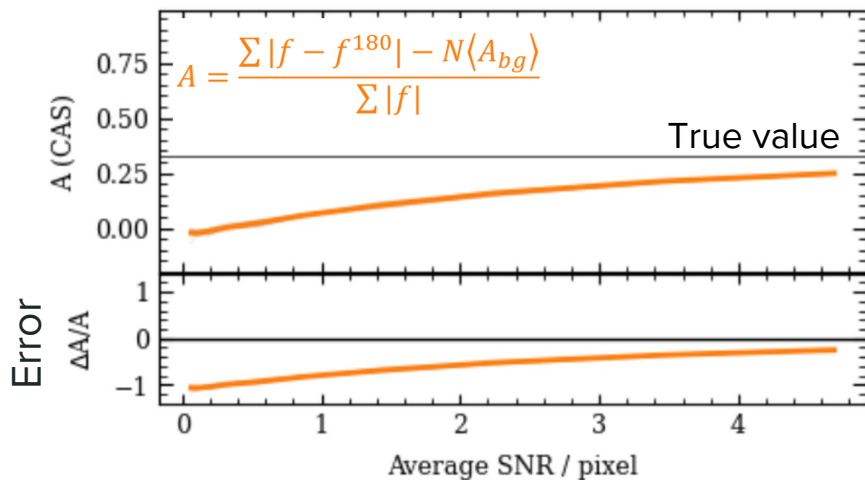
Normalization used to include a non-zero noise contribution, making asymmetry aperture size-dependent

Better behaviour with noisy images

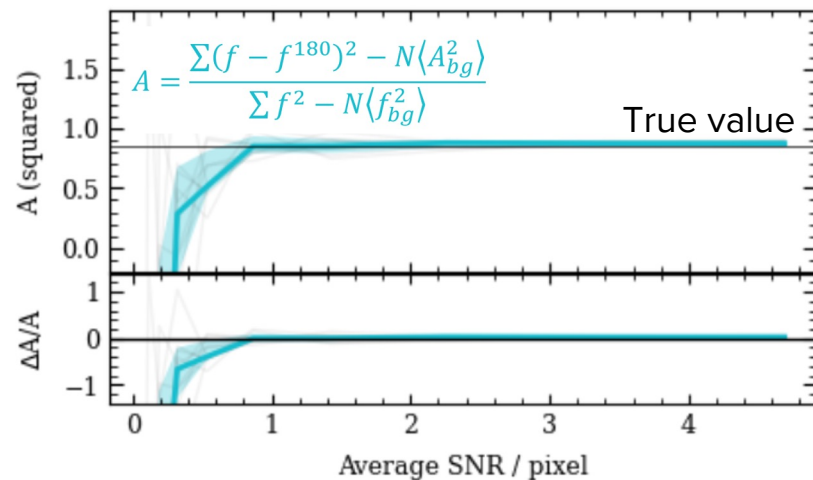
Gaussian noise completely decoupled from the source asymmetry

Asymmetry squared

CAS asymmetry

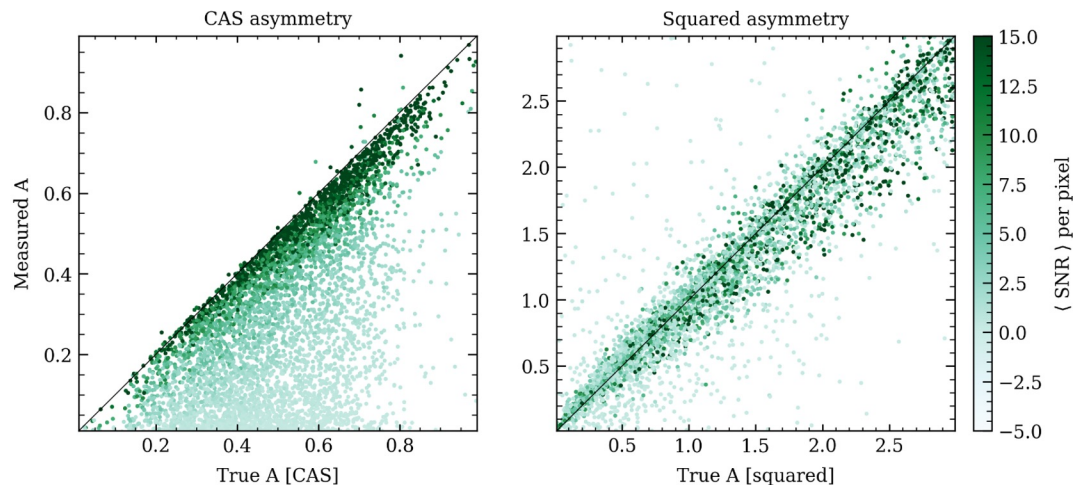


Squared asymmetry



Asymmetry squared

$$A = \frac{\sum (f - f^{180})^2 - N \langle A_{bg}^2 \rangle}{\sum f^2 - N \langle f_{bg}^2 \rangle}$$



Better normalization

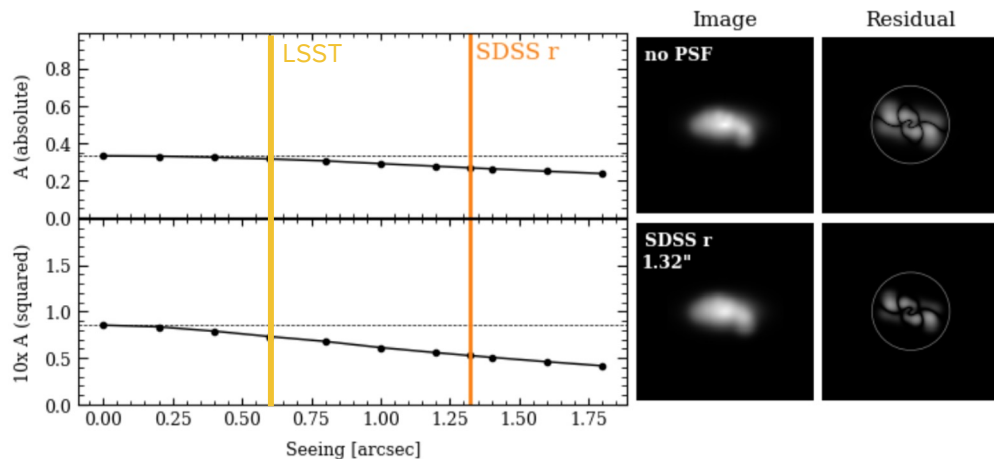
Normalization used to include a non-zero noise contribution, making asymmetry aperture size-dependent

Better behaviour with noisy images

Gaussian noise completely decoupled from the source asymmetry

Asymmetry squared: *PSF*

$$A = \frac{\sum (f - f^{180})^2 - N \langle A_{bg}^2 \rangle}{\sum f^2 - N \langle f_{bg}^2 \rangle}$$



Worse at very low SNR

background flux normalization
makes the denominator ~ 0
when background flux dominates

Worse behaviour with PSF

flux² responds strongly to
re-distribution of flux via seeing

Fourier

Asymmetry squared

$$f = \underset{\text{PSF}}{\lambda} * \overset{\text{source}}{f_s} + \underset{\text{noise}}{\sigma}$$

Fourier facts

1. Power ($\sum f^2$) in image space and image space are the same
2. Convolution in Fourier space is multiplication \Rightarrow separable

Fourier

Asymmetry squared

1 $A^2(\text{source}) = A^2(\mathcal{F}[\text{source}])$

$$f = \underset{\text{PSF}}{\lambda} * \overset{\text{source}}{f_s} + \underset{\text{noise}}{\sigma}$$

Fourier facts

1. Power ($\sum f^2$) in image space and image space are the same
2. Convolution in Fourier space is multiplication \Rightarrow separable

Fourier

Asymmetry squared

1 $A^2(\text{source}) = A^2(\mathcal{F}[\text{source}])$

2 $\mathcal{F}[\text{source}] = H \times \mathcal{F}[\text{image}]$

$$H = \frac{1 + \text{SNR}^{-2}}{\lambda^2 + \text{SNR}^{-2}}$$

PSF signal-to-noise

$$f = \lambda * f_s + \sigma$$

source noise

Fourier facts

1. Power ($\sum f^2$) in image space and image space are the same
2. Convolution in Fourier space is multiplication \Rightarrow separable

Fourier

Asymmetry squared

- 1 $A^2(\text{source}) = A^2(\mathcal{F}[\text{source}])$
- 2 $\mathcal{F}[\text{source}] = H \times \mathcal{F}[\text{image}]$

The rest of the calculation as usual, but in Fourier space!

$$A = \frac{\sum (f - f^{180})^2 - N \langle A_{bg}^2 \rangle}{\sum f^2 - N \langle f_{bg}^2 \rangle}$$

Better normalization

Normalization used to include a non-zero noise contribution, making asymmetry aperture size-dependent

Corrects for noise

Gaussian noise completely decoupled from the source asymmetry

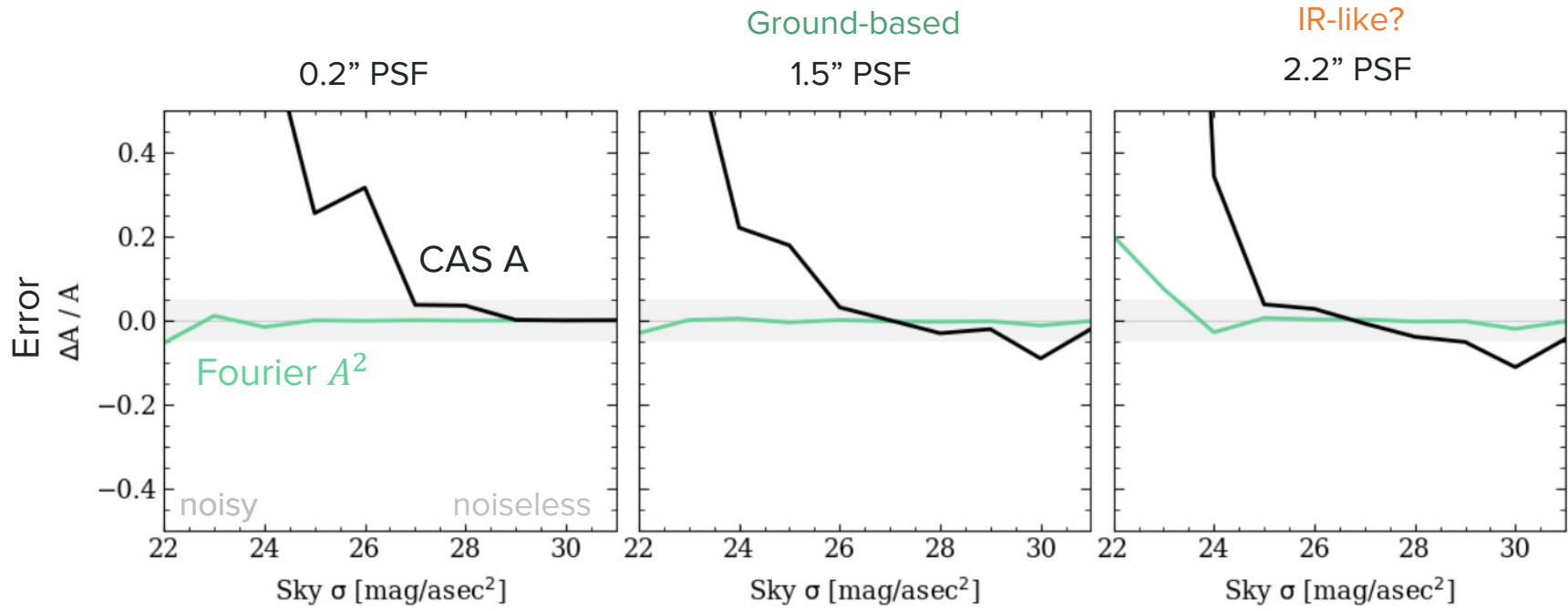
Corrects for PSF

In Fourier space, PSF can be decoupled. We calculate A in Fourier space -

no deconvolution!

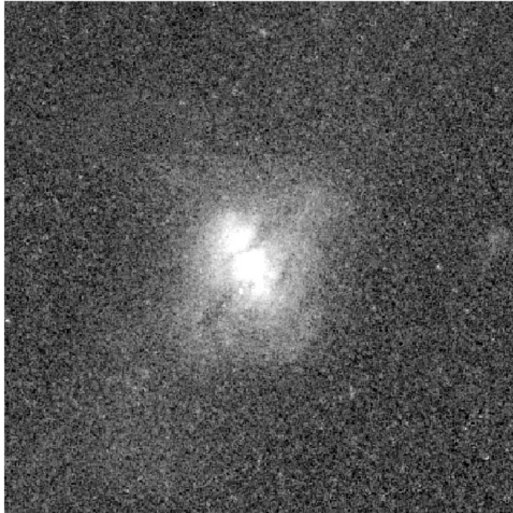
Fourier

Asymmetry squared



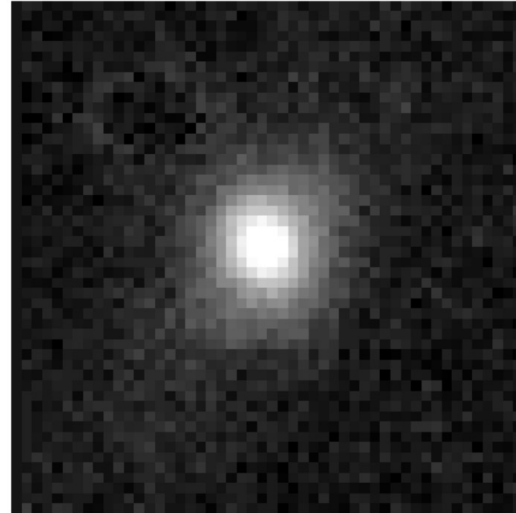
Still work in progress, but...

HST *R*-band



$A = 0.35$

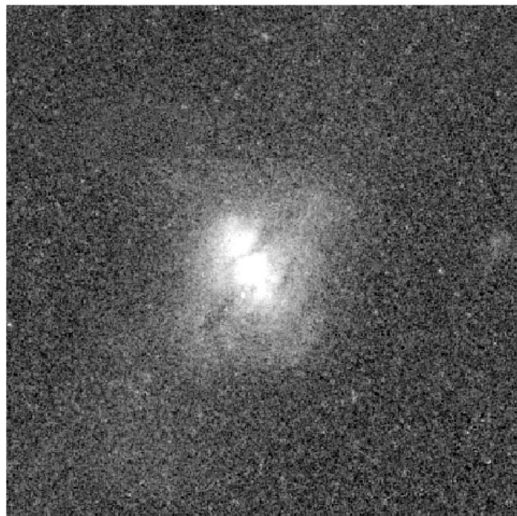
SDSS *r*-band



$A = 0.11$

Still work in progress, but...

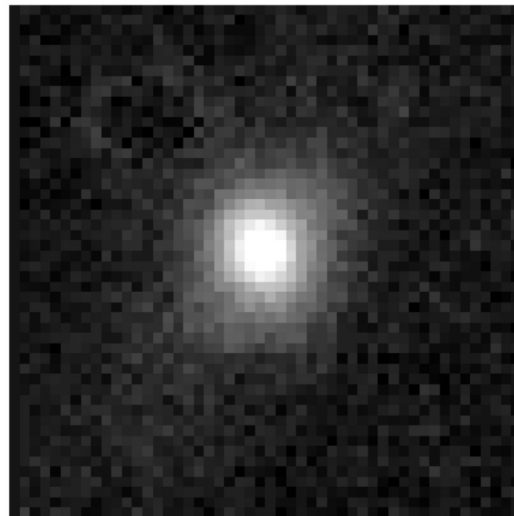
HST *R*-band



$$A = 0.35$$

$$\mathcal{F}[A^2] = 1.61$$

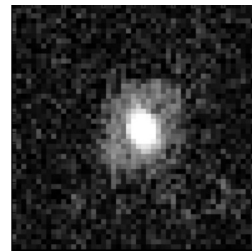
SDSS *r*-band



$$A = 0.11$$

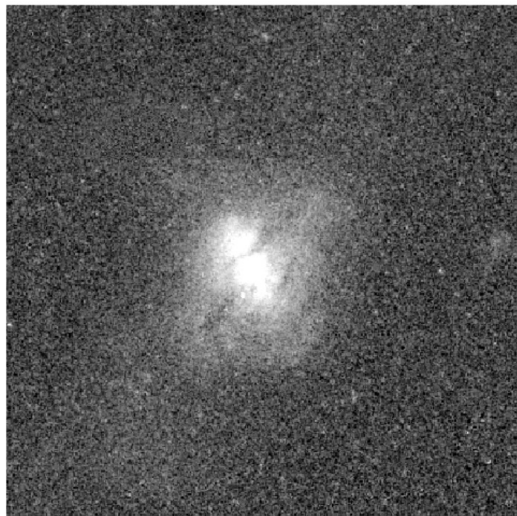
$$\mathcal{F}[A^2] = 1.29$$

Deconvolved



Still work in progress, but...

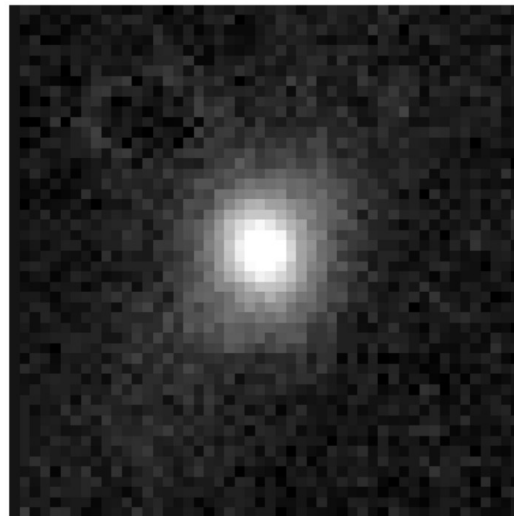
HST *R*-band



$A = 0.35$

$\mathcal{F}[A^2] = 1.61$

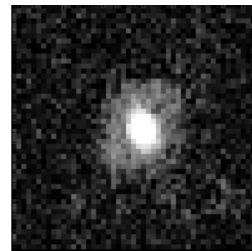
SDSS *r*-band



$A = 0.11$

$\mathcal{F}[A^2] = 1.29$

Deconvolved



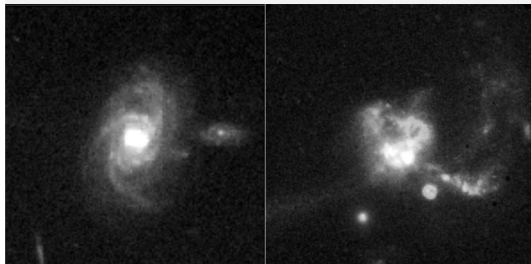
70% error

20% error

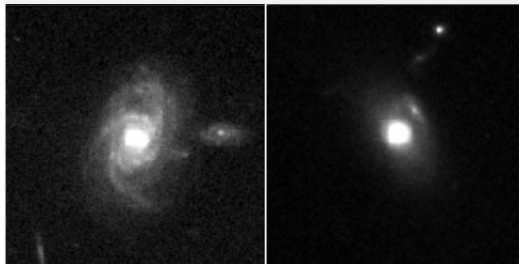
almost

So asymmetry is great again, what next?

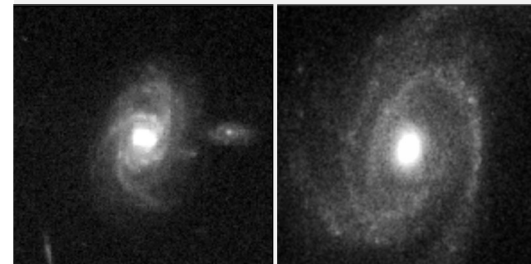
Disturbance



Bulge strength



Size



Non
parametric

Asymmetry

Shape asymmetry

G/M_{20}

Shape

Concentration

G/M_{20} bulge strength

Petrosian radius

Compactness

Model
dependent

Residual Flux Fraction [RFF]

Sérsic index

Bulge-to-disk ratio [B/T]

Gotta test 'em all!
Long overdue – stay tuned 😊

Quantitative morphology with ML

Faster and even more robust!



Disk / bulge strength

C, Sersic n, B/T

Tidal features

A_s, outer A

Internal disturbances
(e.g. dust lanes)

A + A_s in different bands

Different merger stages

A, A_s, G/M20

Work plan

1. Statistically test common morphology measurements. Long overdue!
 - Evaluate response to noise + seeing
 - See if improvements can be made to algorithms
 - Edit **statmorph** (open-source morphology code)
2. Train a neural network to *quickly* measure their *traditional* values
Easy to use by community right away after the initial data release
3. Train a neural network to *robustly* measure *intrinsic* values
These values should be consistent across all data releases

Thank you!
